

**NP-3573(CV-III)**  
**B.Sc. (Computer Science)**  
**Examination, Dec.-2021**

**APPLIED MATHEMATICS - I**  
**(BCS-102)**

*Time : 1½ Hours ] [Maximum Marks : 75*

**Note :** Attempt questions from all Sections  
as per instructions.

**Section-A**

**(Very Short Answer Questions)**

**Note :** Attempt any **two** questions. Each  
question carries 7.5 marks.

$$2 \times 7.5 = 15$$

1. Find the differential coefficient of  $e^{2x} \sin^3 x$ .
2. Find the Jacobian  $J(u, v)$  for

$$u = e^x \sin y, v = x \log \sin y.$$

3. Find the inverse of the matrix by elementary transformation.

$$A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$$

4. Find  $\iint_R f(x, y) dA$  for  $f(x, y) = 1 - 6x^2y$

and R.I.  $0 \leq x \leq 2, -1 \leq y \leq 1$ .

5. Find the magnitude of the gradient of the function  $f = xyz^3$  at  $(1, 0, 2)$ .

**Section-B**

**(Short Answer Questions)**

**Note :** Attempt any **one** question. Each  
question carries 15 marks.  $1 \times 15 = 15$

6.  $u = \sin^{-1} \left( \frac{x^2 + y^2}{x + y} \right)$  show that

$$x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \tan u$$

7. Prove that  $x^5 - 5x^4 + 5x^3 - 10$  has a maximum for  $x = 1$ , a minimum for  $x = 3$  and for  $x = 0$ , it has neither a maximum

nor a minimum.

8. Reduce the matrix A to canonical form

and find its rank:

$$A = \begin{bmatrix} 2 & -1 & 3 & 3 \\ 0 & 3 & 4 & 1 \\ 2 & 3 & 7 & 4 \\ 2 & 5 & 11 & 5 \end{bmatrix}$$

### Section-C

#### (Detailed Answer Questions)

**Note :** Attempt any **two** questions. Each question carries 22.5 marks.

$$2 \times 22.5 = 45$$

9. (a) Find Taylor's Series expansion of  $f(xy) = x^3 + xy^2$  about point (2, 1).  
(b) Expand  $\log(1+x)$  in powers of  $x$ .
10. Use the method of Lagrange's multipliers to find the volume of the largest rectangular parallelepiped that can be inscribed in the ellipsoid

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

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P.T.O.

11. State Cayley-Hamilton theorem. Find the eigen values and eigen vectors of the

matrix

$$A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$

12. (a) By changing the order of integration

$$\text{Evaluate } \int_0^1 \int_{x^2}^{2-x} xy \, dy \, dx$$

(b) Define Beta and Gamma function.

Establish the relation between Beta and Gamma function

$$\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$$

13. (a) Define curl of a vector. Prove the following vector identity:

$$\text{div}(\vec{u} \times \vec{v}) = \vec{v} \cdot \text{curl} \vec{u} - \vec{u} \cdot \text{curl} \vec{v}$$

(b) State Gauss divergence theorem. Use Gauss divergence theorem in Cartesian form to evaluate

$$\iint_S x \, dy \, dz + y \, dz \, dx + z \, dx \, dy,$$

where the surface S is the sphere

$$x^2 + y^2 + z^2 = a^2.$$

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