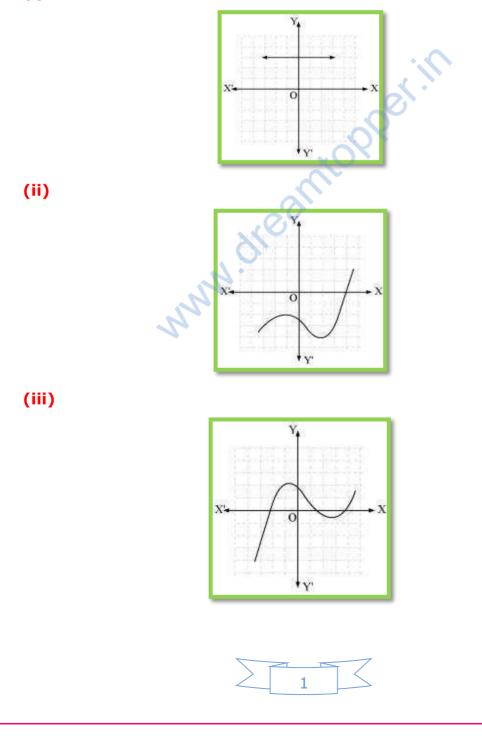
Mathematics

(Chapter – 2) (Polynomials) (Class – X)

Exercise 2.1

Question 1:

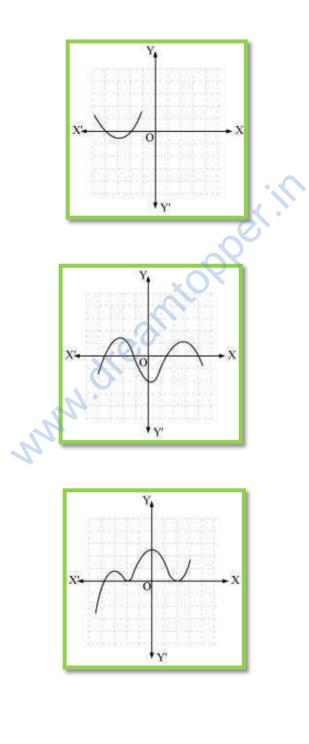
The graphs of y = p(x) are given in following figure, for some polynomials p(x). Find the number of zeroes of p(x), in each case. (i)





(v)

(v)



2

Answer 1:

- (i) The number of zeroes is 0 as the graph does not cut the x-axis at any point.
- (ii) The number of zeroes is 1 as the graph intersects the *x*-axis at only 1 point.
- (iii) The number of zeroes is 3 as the graph intersects the *x*-axis at 3 points.
- (iv) The number of zeroes is 2 as the graph intersects the *x*-axis at 2 points.

(v) The number of zeroes is 4 as the graph intersects the *x*-axis at 4 points.

(vi) The number of zeroes is 3 as the graph intersects the x-axis at 3 points.



Mathematics

(Chapter – 2) (Polynomials) (Class X)

Exercise 2.2

Question 1:

Find the zeroes of the following quadratic polynomials and verify the relationship between the zeroes and the coefficients.

 $(iii)6x^2 - 3 - 7x$ $(i)x^2 - 2x - 8$ (ii) $4s^2 - 4s + 1$ $(v)t^2 - 15$ $(vi)3x^2 - x - 4$ $(iv)4u^2 + 8u$ Answer 1: $x^{2}-2x-8 = (x-4)(x+2)$ (i) The value of $x^2 - 2x - 8$ is zero when x - 4 = 0 or x + 2 = 0, i.e., when x = 4 or x = -2Therefore, the zeroes of $x^2 - 2x - 8$ are 4 and -2Sum of zeroes = $4-2=2=\frac{-(-2)}{1}=\frac{-(\text{Coefficient of }x)}{\text{Coefficient of }x^2}$ Product of zeroes $= 4 \times (-2) = -8 = \frac{(-8)}{1} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$ (ii) $4s^2 - 4s + 1 = (2s - 1)^2$ The value of $4s^2 - 4s + 1$ is zero when 2s - 1 = 0, i.e., $s = \frac{1}{2}$ Therefore, the zeroes of $4s^2 - 4s + 1$ are $\frac{1}{2}$ and $\frac{1}{2}$. Sum of zeroes = $\frac{1}{2} + \frac{1}{2} = 1 = \frac{-(-4)}{4} = \frac{-(\text{Coefficient of } s)}{(\text{Coefficient of } s^2)}$ Product of zeroes $=\frac{1}{2} \times \frac{1}{2} = \frac{1}{4} = \frac{\text{Constant term}}{\text{Coefficient of }s^2}$ (iii) $6x^2 - 3 - 7x = 6x^2 - 7x - 3 = (3x+1)(2x-3)$

The value of $6x^2 - 3 - 7x$ is zero when 3x + 1 = 0 or 2x - 3 = 0, i.e.,

$$x = \frac{-1}{3}$$
 or $x = \frac{3}{2}$

Therefore, the zeroes of $6x^2 - 3 - 7x$ are $\frac{-1}{3}$ and $\frac{3}{2}$. Sum of zeroes = $\frac{-1}{3} + \frac{3}{2} = \frac{7}{6} = \frac{-(-7)}{6} = \frac{-(\text{Coefficient of } x)}{\text{Coefficient of } x^2}$ Product of zeroes = $\frac{-1}{3} \times \frac{3}{2} = \frac{-1}{2} = \frac{-3}{6} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$

(iv)
$$4u^2 + 8u = 4u^2 + 8u + 0$$

= $4u(u+2)$

The value of $4u^2 + 8u$ is zero when 4u = 0 or u + 2 = 0, i.e., u = 0 or u = -2

Therefore, the zeroes of $4u^2 + 8u$ are 0 and -2.

Sum of zeroes = $0 + (-2) = -2 = \frac{-(8)}{4} = \frac{-(\text{Coefficient of } u)}{\text{Coefficient of } u^2}$ Product of zeroes = $0 \times (-2) = 0 = \frac{0}{4} = \frac{\text{Constant term}}{\text{Coefficient of } u^2}$

(v) $t^2 - 15$ $=t^2 - 0t - 15$ $=(t-\sqrt{15})(t+\sqrt{15})$

The value of $t^2 - 15$ is zero when $t - \sqrt{15} = 0$ or $t + \sqrt{15} = 0$, i.e., when $t = \sqrt{15}$ or $t = -\sqrt{15}$

Therefore, the zeroes of $t^2 - 15$ are $\sqrt{15}$ and $-\sqrt{15}$.

Sum of zeroes = $\sqrt{15} + (-\sqrt{15}) = 0 = \frac{-0}{1} = \frac{-(\text{Coefficient of } t)}{(\text{Coefficient of } t^2)}$ Product of zeroes = $(\sqrt{15})(-\sqrt{15}) = -15 = \frac{-15}{1} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$

(vi) $3x^2 - x - 4$ = (3x - 4)(x + 1)

The value of $3x^2 - x - 4$ is zero when 3x - 4 = 0 or x + 1 = 0, i.e.,

when
$$x = \frac{4}{3}$$
 or $x = -1$

Therefore, the zeroes of $3x^2 - x - 4$ are 4/3 and -1.

Sum of zeroes =
$$\frac{4}{3} + (-1) = \frac{1}{3} = \frac{-(-1)}{3} = \frac{-(\text{Coefficient of } x)}{\text{Coefficient of } x^2}$$

Product of zeroes = $\frac{4}{3}(-1) = \frac{-4}{3}$

Product of zeroes $=\frac{4}{3}(-1)=\frac{-4}{3}$ Coefficient of x^2

Question 2:

Find a quadratic polynomial each with the given numbers as the sum and product of its zeroes respectively.

(i) $\frac{1}{4}$, -1 (ii) $\sqrt{2}$, $\frac{1}{3}$ (iii) 0, $\sqrt{5}$ (iv) 1,1 (v) $-\frac{1}{4}$, $\frac{1}{4}$ (vi) 4,1

Answer 2:

(i) $\frac{1}{4}, -1$

Let the polynomial be $ax^2 + bx + c$ and its zeroes be α and β .

$$\alpha + \beta = \frac{1}{4} = \frac{-b}{a}$$
$$\alpha \beta = -1 = \frac{-4}{4} = \frac{c}{a}$$
If $a = 4$, then $b = -1$, $c = -4$

Therefore, the quadratic polynomial is $4x^2 - x - 4$.

(ii)
$$\sqrt{2}, \frac{1}{3}$$

Let the polynomial be $ax^2 + bx + c$ and its zeroes be α and β .

$$\alpha + \beta = \sqrt{2} = \frac{3\sqrt{2}}{3} = \frac{-b}{a}$$

$$\alpha\beta = \frac{1}{3} = \frac{c}{a}$$

If $a = 3$, then $b = -3\sqrt{2}$, $c = 1$

Therefore, the quadratic polynomial is $3x^2 - 3\sqrt{2}x + 1$.

(iii) $0,\sqrt{5}$

Let the polynomial be $ax^2 + bx + c$ and its zeroes be α and β .

$$\alpha + \beta = 0 = \frac{0}{1} = \frac{-b}{a}$$
$$\alpha \times \beta = \sqrt{5} = \frac{\sqrt{5}}{1} = \frac{c}{a}$$
If $a = 1$, then $b = 0$, $c = \sqrt{5}$

Therefore, the quadratic polynomial is $x^2 + \sqrt{5}$.

(iv) 1, 1

Let the polynomial be $ax^2 + bx + c$ and its zeroes be α and β .

$$\alpha + \beta = 1 = \frac{1}{1} = \frac{-b}{a}$$
$$\alpha \times \beta = 1 = \frac{1}{1} = \frac{c}{a}$$
If $a = 1$, then $b = -1$, $c = 1$

Therefore, the quadratic polynomial is $x^2 - x + 1$.

 $(v) \quad -\frac{1}{4}, \frac{1}{4}$

Let the polynomial be $ax^2 + bx + c$ and its zeroes be α and β .

$$\alpha + \beta = \frac{-1}{4} = \frac{-b}{a}$$

$$\alpha \times \beta = \frac{1}{4} = \frac{c}{a}$$

If $a = 4$, then $b = 1$, $c = 1$

Therefore, the quadratic polynomial is $4x^2 + x + 1$.

(vi) 4, 1

Let the polynomial be $ax^2 + bx + c$ and its zeroes be α and β .

$$\alpha + \beta = 4 = \frac{4}{1} = \frac{-b}{a}$$
$$\alpha \times \beta = 1 = \frac{1}{1} = \frac{c}{a}$$
If $a = 1$, then $b = -4$, $c = 1$

Therefore, the quadratic polynomial is $x^2 - 4x + 1$.

Mathematics

(Chapter - 2) (Polynomials) (Class – X)

Exercise 2.3

Question 1:

Divide the polynomial p(x) by the polynomial g(x) and find the quotient and remainder in each of the following:

1

(i) $p(x) = x^3 - 3x^2 + 5x - 3$, $g(x) = x^2 - 2$ (i) $p(x) = x^4 - 3x^2 + 4x + 5$, $g(x) = x^2 + 1 - x$ (ii) $p(x) = x^4 - 5x + 6$, $g(x) = 2 - x^2$ (iii) $p(x) = x^4 - 5x + 6$, $g(x) = 2 - x^2$ Answer 1: (i) $p(x) = x^3 - 3x^2 + 5x - 3$

Quotient = x - 3

Remainder = 7x - 9

(ii)
$$p(x) = x^4 - 3x^2 + 4x + 5 = x^4 + 0 \cdot x^3 - 3x^2 + 4x + 5$$

 $q(x) = x^2 + 1 - x = x^2 - x + 1$

$$\begin{array}{r} x^{2} + x - 3 \\ x^{2} - x + 1) x^{4} + 0 x^{3} - 3x^{2} + 4x + 5 \\ x^{4} - x^{3} + x^{2} \\ - + - \\ \hline x^{3} - 4x^{2} + 4x + 5 \\ x^{3} - x^{2} + x \\ - + - \\ \hline - 3x^{2} + 3x + 5 \\ -3x^{2} + 3x - 3 \\ + - + \\ \hline 8 \end{array}$$

Quotient = $x^2 + x - 3$

Remainder = 8



(iii)
$$p(x) = x^4 - 5x + 6 = x^4 + 0.x^2 - 5x + 6$$

 $q(x) = 2 - x^2 = -x^2 + 2$
 $-x^2 + 2) \xrightarrow{-x^2 - 2} x^4 + 0.x^2 - 5x + 6$
 $x^4 - 2x^2$
 $- + \frac{-x^2 - 5x + 6}{2x^2 - 5x + 6}$
 $2x^2 - 4$
 $- \frac{-x^2 - 5x + 10}{2x^2 - 5x + 10}$

 $e^{-x^2 - 2}$ Remainder = -5x + 10Question 2:

Check whether the first polynomial is a factor of the second polynomial by dividing the second polynomial by the first polynomial:

(i)
$$t^2 - 3, 2t^4 + 3t^3 - 2t^2 - 9t - 12$$

(ii)
$$x^2 + 3x + 1, 3x^4 + 5x^3 - 7x^2 + 2x + 2$$

(iii) $x^3 - 3x + 1, x^5 - 4x^3 + x^2 + 3x + 1$

Answer 2:

(i) $t^2 - 3$, $2t^4 + 3t^3 - 2t^2 - 9t - 12$



$$\begin{array}{r}
 + + + \\
 2x^2 + 6x + 2 \\
 2x^2 + 6x + 2 \\
 0
 \end{array}$$

Since the remainder is 0,

4

Hence,
$$x^{2} + 3x + 1$$
 is a factor of $3x^{4} + 5x^{3} - 7x^{2} + 2x + 2$.
(iii) $x^{3} - 3x + 1$, $x^{5} - 4x^{3} + x^{2} + 3x + 1$
 $x^{3} - 3x + 1$) $x^{5} - 4x^{3} + x^{2} + 3x + 1$
 $x^{5} - 3x^{3} + x^{2}$
 $- + -$
 $-x^{3} + 3x - 1$
 $+ - - +$
2
Since the remainder $\neq 0$,
Hence, $x^{3} - 3x + 1$ is not a factor of $x^{5} - 4x^{3} + x^{2} + 3x + 1$
Question 3:

Question 3:

Obtain all other zeroes of $3x^4 + 6x^3 - 2x^2 - 10x - 5$, if two of its zeroes are

$$\sqrt{\frac{5}{3}}$$
 and $-\sqrt{\frac{5}{3}}$

Answer 3:

$$p(x) = 3x^4 + 6x^3 - 2x^2 - 10x - 5$$

Since the two zeroes are $\sqrt{\frac{5}{3}}$ and $-\sqrt{\frac{5}{3}}$ $\therefore \left(x - \sqrt{\frac{5}{3}}\right) \left(x + \sqrt{\frac{5}{3}}\right) = \left(x^2 - \frac{5}{3}\right)$ is a factor of $3x^4 + 6x^3 - 2x^2 - 10x - 5$

Therefore, we divide the given polynomial by $x^2 - \frac{5}{3}$



$$x^{2} + 0.x - \frac{5}{3} \underbrace{) \begin{array}{l} 3x^{2} + 6x + 3 \\ 3x^{4} + 6x^{3} - 2x^{2} - 10x - 5 \\ 3x^{4} + 0x^{3} - 5x^{2} \\ \hline - - + \\ 6x^{3} + 3x^{2} - 10x - 5 \\ 6x^{3} + 0x^{2} - 10x \\ \hline - - + \\ 3x^{2} + 0x - 5 \\ \hline 3x^{2} + 0x - 5 \\ \hline - - + \\ \hline 0 \\ 3x^{4} + 6x^{3} - 2x^{2} - 10x - 5 = \left(x^{2} - \frac{5}{3}\right)(3x^{2} + 6x + 3) \\ = 3\left(x^{2} - \frac{5}{3}\right)(x^{2} + 2x + 1)$$

We factorize $x^2 + 2x + 1$ = $(x+1)^2$

Therefore, its zero is given by x + 1 = 0 or x = -1As it has the term $(x+1)^2$, therefore, there will be 2 zeroes at x = -1.

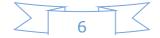
Hence, the zeroes of the given polynomial are $\sqrt{\frac{5}{3}}$, $-\sqrt{\frac{5}{3}}$ -1 and -1.

Question 4:

On dividing $x^3 - 3x^2 + x + 2$ by a polynomial g(x), the quotient and remainder were x - 2 and -2x + 4, respectively. Find g(x).

Answer 4:

 $p(x) = x^3 - 3x^2 + x + 2 \qquad \text{(Dividend)}$



g(x) = ? (Divisor) Quotient = (x - 2)Remainder = (-2x + 4)Dividend = Divisor × Quotient + Remainder $x^{3}-3x^{2}+x+2=g(x)\times(x-2)+(-2x+4)$ $x^{3}-3x^{2}+x+2+2x-4=g(x)(x-2)$ $x^{3}-3x^{2}+3x-2=g(x)(x-2)$

$$g(x) \text{ is the quotient when we divide } \left(x^3 - 3x^2 + 3x - 2\right) \text{ by } (x-2)$$

$$x-2) \overline{x^3 - 3x^2 + 3x - 2}$$

$$x^3 - 2x^2$$

$$- +$$

$$-x^2 + 3x - 2$$

$$-x^2 + 2x$$

$$+ -$$

$$x-2$$

$$x-$$

Question 5:

Give examples of polynomial p(x), g(x), q(x) and r(x), which satisfy the division algorithm and

(i) deg $p(x) = \deg q(x)$

(ii) deg $q(x) = \deg r(x)$



(iii) deg r(x) = 0

Answer 5:

According to the division algorithm, if p(x) and g(x) are two polynomials with $g(x) \neq 0$, then we can find polynomials q(x) and r(x) such that $p(x) = g(x) \times q(x) + r(x)$,

where r(x) = 0 or degree of r(x) < degree of <math>g(x)

Degree of a polynomial is the highest power of the variable in the polynomial.

(i) deg p(x) = deg q(x)

Degree of quotient will be equal to degree of dividend when divisor is constant (i.e., when any polynomial is divided by a constant).

Let us assume the division of $6x^2 + 2x + 2$ by 2.

Here, $p(x) = 6x^2 + 2x + 2$

$$g(x) = 2$$

 $q(x) = 3x^2 + x + 1$ and r(x) = 0

Degree of p(x) and q(x) is the same i.e., 2. Checking for division algorithm, $p(x) = g(x) \times q(x) + r(x)$

 $6x^2 + 2x + 2 = (2)(3x^2 + x + 1) + 0$

Thus, the division algorithm is satisfied.

(ii) deg q(x) = deg r(x)Let us assume the division of $x^3 + x$ by x^2 , Here, $p(x) = x^3 + x g(x) = x^2 q(x) = x$ and r(x) = xClearly, the degree of q(x) and r(x) is the same i.e., 1. Checking for division algorithm, $p(x) = g(x) \times q(x) + r(x)$ $x^3 + x = (x^2) \times x + x x^3 + x = x^3 + x$

Thus, the division algorithm is satisfied.

(iii)deg r(x) = 0

Degree of remainder will be 0 when remainder comes to a constant.

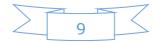
Let us assume the division of $x^3 + 1$ by x^2 .

Here, $p(x) = x^3 + 1 g(x) = x^2 q(x) = x$ and r(x) = 1

Clearly, the degree of r(x) is 0. Checking for division algorithm,

 $p(x) = g(x) \times q(x) + r(x) x^3 + 1 = (x^2) \times x + 1 x^3 + 1 = x^3 + 1$

Thus, the division algorithm is satisfied.



Mathematics

(Chapter - 2) (Polynomials) (Class – X)

Exercise 2.4

Question 1:

Verify that the numbers given alongside of the cubic polynomials below are their zeroes. Also verify the relationship between the zeroes and the coefficients in each case:

(i) $2x^3 + x^2 - 5x + 2; \frac{1}{2}, 1, -2$

(ii)
$$x^3 - 4x^2 + 5x - 2;$$
 2,1,1

(i)
$$x^{3} - 4x^{2} + 5x - 2;$$
 2,1,1
Answer 1:
(i) $p(x) = 2x^{3} + x^{2} - 5x + 2.$
Zeroes for this polynomial are $\frac{1}{2}$, 1, -2
 $p(\frac{1}{2}) = 2(\frac{1}{2})^{3} + (\frac{1}{2})^{2} - 5(\frac{1}{2}) + 2$
 $= \frac{1}{4} + \frac{1}{4} - \frac{5}{2} + 2$
 $= 0$
 $p(1) = 2 \times 1^{3} + 1^{2} - 5 \times 1 + 2$
 $= 0$
 $p(-2) = 2(-2)^{3} + (-2)^{2} - 5(-2) + 2$
 $= -16 + 4 + 10 + 2 = 0$

Therefore, $\frac{1}{2}$, 1, and -2 are the zeroes of the given polynomial. Comparing the given polynomial with $ax^3 + bx^2 + cx + d$, we obtain a = 2, b = 1, c = -5, d = 2



We can take $\alpha = \frac{1}{2}, \beta = 1, \gamma = -2$ $\alpha + \beta + \gamma = \frac{1}{2} + 1 + (-2) = -\frac{1}{2} = \frac{-b}{\alpha}$ $\alpha\beta + \beta\gamma + \alpha\gamma = \frac{1}{2} \times 1 + 1(-2) + \frac{1}{2}(-2) = \frac{-5}{2} = \frac{c}{\alpha}$ $\alpha\beta\gamma = \frac{1}{2} \times 1 \times (-2) = \frac{-1}{1} = \frac{-(2)}{2} = \frac{-d}{a}$

Therefore, the relationship between the zeroes and the coefficients is dreamtopper verified.

 $p(x) = x^3 - 4x^2 + 5x - 2$ (ii) Zeroes for this polynomial are 2, 1, 1.

$$p(2) = 2^{3} - 4(2^{2}) + 5(2) - 2$$

= 8 - 16 + 10 - 2 = 0
$$p(1) = 1^{3} - 4(1)^{2} + 5(1) - 2$$

= 1 - 4 + 5 - 2 = 0

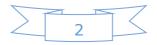
Therefore, 2, 1, 1 are the zeroes of the given polynomial. Comparing the given polynomial with $ax^3 + bx^2 + cx + d$, we obtain a = 1, b = -4, c = 5, d = -2.

Verification of the relationship between zeroes and coefficient of the given polynomial

Sum of zeroes = $2+1+1=4=\frac{-(-4)}{1}=\frac{-b}{2}$

Multiplication of zeroes taking two at a time

 $= (2)(1) + (1)(1) + (2)(1) = 2 + 1 + 2 = 5 = \frac{(5)}{1} = \frac{c}{a}$ Multiplication of zeroes = $2 \times 1 \times 1 = 2$ = $\frac{-(-2)}{1} = \frac{-d}{2}$



Hence, the relationship between the zeroes and the coefficients is verified.

Question 2:

Find a cubic polynomial with the sum, sum of the product of its zeroes taken two at a time, and the product of its zeroes as 2, -7, -14 respectively.

Answer 2:

Let the polynomial be $ax^3 + bx^2 + cx + d$ and the zeroes be α, β , and γ

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It is given that

$$\alpha + \beta + \gamma = \frac{2}{1} = \frac{-b}{a}$$
$$\alpha\beta + \beta\gamma + \alpha\gamma = \frac{-7}{1} = \frac{c}{a}$$
$$\alpha\beta\gamma = \frac{-14}{1} = \frac{-d}{a}$$

If a = 1, then b = -2, c = -7, d = 14Hence, the polynomial is $x^{3}-2x^{2}-7x+14$.

Question 3:

If the zeroes of polynomial, $x^3 - 3x^2 + x + 1$ are a - b, a, a + b find a and b.

Answer 3:

 $p(x) = x^3 - 3x^2 + x + 1$ Zeroes are a - b, a + a + bComparing the given polynomial with $px^3 + qx^2 + rx + t$, we obtain p = 1, q = -3, r = 1, t = 1



Sum of zeroes = a - b + a + a + b

$$\frac{-q}{p} = 3a$$
$$\frac{-(-3)}{1} = 3a$$
$$3 = 3a$$
$$a = 1$$

The zeroes are 1-b, 1, 1+b

$$\frac{-t}{p} = 1 - b^2$$
$$\frac{-1}{1} = 1 - b^2$$
$$1 - b^2 = -1$$
$$1 + 1 = b^2$$
$$b = \pm \sqrt{2}$$

 $a \pm \sqrt{2}$ Hence, a = 1 and $b = \sqrt{2}$ or $-\sqrt{2}$ **Cuestion 4:**It two zeroes of the r
id other zero] It two zeroes of the polynomial , $x^4 - 6x^3 - 26x^2 + 138x - 35$ are $2 \pm \sqrt{3}$

Answer 4:

Given 2 + $\sqrt{3}$ and 2 - $\sqrt{3}$ are zeroes of the given polynomial. So, $(2 + \sqrt{3})(2 - \sqrt{3})$ is a factor of polynomial. Therefore, $[x - (2 + \sqrt{3})][x - (2 - \sqrt{3})] = x^2 + 4 - 4x - 3$ $= x^2 - 4x + 1$ is a factor of the given polynomial For finding the remaining zeroes of the given polynomial, we will find

4

$$\frac{x^{2}-2x-35}{x^{4}-6x^{3}-26x^{2}+138x-35}$$

$$x^{4}-4x^{3}+x^{2}$$

$$\frac{-+-}{-2x^{3}-27x^{2}+138x-35}$$

$$-2x^{3}+8x^{2}-2x$$

$$\frac{+--+}{-35x^{2}+140x-35}$$

$$-35x^{2}+140x-35$$

$$\frac{+--+}{0}$$
Clearly, $x^{4}-6x^{3}-26x^{2}+138x-35 = (x^{2}-4x+1)(x^{2}-2x-35)$

Clearly,
$$x^4 - 6x^3 - 26x^2 + 138x - 35 = (x^2 - 4x + 1)(x^2 - 2x - 35)$$

 $(x^2-2x-35)$ is also a factor of the given

It can be observed that polynomial $(x^2-2x-35) = (x-7)(x+5)$

Therefore, the value of the polynomial is also zero when x-7=0 or x + 5 = 0

Or x = 7 or -5

Hence, 7 and -5 are also zeroes of this polynomial.

Question 5:

If the polynomial $x^4 - 6x^3 + 16x^2 - 25x + 10$ is divided by another polynomial, $x^2 - 2x + k$ the remainder comes out to be x + a, find k and а.



Answer 5:

By division algorithm, Dividend = Divisor × Quotient + Remainder Dividend - Remainder = Divisor × Quotient $x^4 - 6x^3 + 16x^2 - 25x + 10 - x - a = x^4 - 6x^3 + 16x^2 - 26x + 10 - a$ will be

divisible by
$$x^2 - 2x + k$$
.
Let us divide $x^4 - 6x^3 + 16x^2 - 26x + 10 - a$ by $x^2 - 2x + k$
 $x^2 - 4x + (8 - k)$
 $x^2 - 2x + k$ $x^4 - 6x^3 + 16x^2 - 26x + 10 - a$
 $x^4 - 2x^3 + kx^2$
 $- + -$
 $-4x^3 + (16 - k)x^2 - 26x$
 $-4x^3 + 8x^2 - 4kx$
 $+ - +$
 $(8 - k)x^2 - (26 - 4k)x + 10 - a$
 $(8 - k)x^2 - (16 - 2k)x + (8k - k^2)$
 $+ -$
 $(-10 + 2k)x + (10 - a - 8k + k^2)$

It can be observed that $(-10+2k)x+(10-a-8k+k^2)$ Will be 0.

Therefore, (-10+2k) = 0 and $(10-a-8k+k^2) = 0$

For (-10+2k) = 0, 2k = 10 And thus, k = 5For $(10-a-8k+k^2) = 0$



 $10 - a - 8 \times 5 + 25 = 0$ 10 - a - 40 + 25 = 0 -5 - a = 0Therefore, a = -5Hence, k = 5 and a = -5

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