Chapter 11
Construction

## Exercise No. 11.1

## Multiple Choice Questions:

1. With the help of a ruler and a compass it is not possible to construct an angle of:
(A) $37.5^{\circ}$
(B) $40^{\circ}$
(C) $22.5^{\circ}$
(D) $67.5^{\circ}$

## Solution:

By using the help of a ruler and a compass, that is possible construct the angels, $90^{\circ}, 60^{\circ}$, $45^{\circ}, 22.5^{\circ}, 30^{\circ}$ etc., and its bisector of an angle. So, it is not possible to construct an angle of $40^{\circ}$.
Hence, the correct option is (B).
2. The construction of a triangle ABC , given that $\mathrm{BC}=\mathbf{6} \mathbf{~ c m}, \angle B=45^{\circ}$ is not possible when difference of $A B$ and $A C$ is equal to:
(A) 6.9 cm
(B) 5.2 cm
(C) 5.0 cm
(D) 4.0 cm

## Solution:

Given: $B C=6 \mathrm{~cm}$ and $\angle B=45^{\circ}$
As, we know that, the construction of a triangle is not possible, if sum of two sides is less than or equal to the third side of the triangle.

So, the difference between other two sides AB and AC should be equal to or greater then BC . Hence, the correct option is (A).
3. The construction of a triangle $\mathbf{A B C}$, given that $\mathbf{B C}=\mathbf{3} \mathbf{~ c m}, \angle C=60^{\circ}$ is possible when difference of $A B$ and $A C$ is equal to:
(A) 3.2 cm
(B) 3.1 cm
(C) 3 cm
(D) 2.8 cm

## Solution:

Given, $\mathrm{BC}=3 \mathrm{~cm}$ and $\angle \mathrm{C}=60^{\circ}$
As, we know that, the construction of a triangle is possible, if sum of two sides is greater than the third side of the triangle.

So, the difference between other two sides AB and AC should not be equal to or greater than BC.
Hence, the correct option is (D).

## Exercise No. 11.2

## Short Answer Questions with Reasoning:

Write True or False in each of the following. Give reasons for your answer:

## 1. An angle of $52.5^{\circ}$ can be constructed.

## Solution:

As, $42.5^{\circ}=\frac{1}{4} \times 210^{\circ}$ and an angle of $210^{\circ}=180^{\circ}+30^{\circ}$ cannot be constructed with the help of ruler and compass.
Hence, the given statement is true.

## 2. An angle of $42.5^{\circ}$ can be constructed.

## Solution:

As, $42.5^{\circ}=\frac{1}{2} \times 85^{\circ}$ and an angle of $85^{\circ}$ cannot be constructed with the help of ruler and compass.
Hence, the given statement is false.
3. A triangle $\mathbf{A B C}$ can be constructed in which $\mathbf{A B}=5 \mathrm{~cm}, \angle \mathrm{~A}=45^{\circ}$ and $\mathbf{B C}$ $+A C=5 \mathrm{~cm}$.

## Solution:

As, a triangle can be constructed, if sum of its two sides is greater than third side.
Here, $\mathrm{BC}+\mathrm{AC}=\mathrm{AB}=5 \mathrm{~cm}$
So, triangle ABC cannot be constructed.
Hence, the given statement is false.
4. A triangle ABC can be constructed in which $\mathrm{BC}=6 \mathbf{~ c m}, \angle \mathrm{C}=30^{\circ}$ and AC $-A B=4 \mathrm{~cm}$.

## Solution:

As, a triangle can be constructed if sum of its two sides is greater than third side.
So, in triangle $\mathrm{ABC}, \mathrm{AB}+\mathrm{BC}>\mathrm{AC}$
$\mathrm{BC}>\mathrm{AC}-\mathrm{AB}$
$6>4$, which is true, so triangle ABC with given conditions can be constructed.
Hence, the given statement is true.
5. A triangle ABC can be constructed in which $\angle \mathrm{B}=105^{\circ}, \angle \mathrm{C}=90^{\circ}$ and AB $+\mathrm{BC}+\mathrm{AC}=10 \mathrm{~cm}$.

## Solution:

Given: $\angle \mathrm{B}=105^{\circ}, \angle \mathrm{C}=90^{\circ}$
We know that, sum of angles of a triangle is $180^{\circ}$.
$\angle \mathrm{A}+\angle \mathrm{B}+\angle \mathrm{C}=180^{\circ}$
Here, $\angle \mathrm{B}+\angle \mathrm{C}=105^{\circ}+90^{\circ}$
$195^{\circ}>180^{\circ}$ which is not true.
Therefore, a triangle ABC with given conditions cannot be constructed.
Hence, the given statement is false.
6. A triangle $A B C$ can be constructed in which $\angle B=60^{\circ}, \angle C=45^{\circ}$ and $A B$ $+\mathrm{BC}+\mathrm{AC}=12 \mathrm{~cm}$.

## Solution:

We know that, sum of angles of a triangle is $180^{\circ}$.
$\angle \mathrm{A}+\angle \mathrm{B}+\angle \mathrm{C}=180^{\circ}$
Here, $\angle \mathrm{B}+\angle \mathrm{C}=60^{\circ}+45^{\circ}=105^{\circ}<180^{\circ}$,
Therefore, a triangle ABC with given conditions can be constructed.
Hence, the given statement is true.

## Exercise No. 11.3

## Short Answer Questions:

1. Draw an angle of $110^{\circ}$ with the help of a protractor and bisect it. Measure each angle.

## Solution:

Given: An angle $\mathrm{AXB}=110^{\circ}$.
To construct: the bisector of angle AXB as follows:


Steps of construction:

1. With $X$ as center and any radius draw an are to intersect the rays $X A$ and $X B$, say at $E$ and D , respectively.
2. With D and E as center's and with the radius more than $\frac{1}{2} \mathrm{DE}$, draw arcs to intersect each other, say at F.
3. Draw the ray XF.

So, ray XF is the required bisector of the angle BXA. On measuring each angle, get:
$\angle \mathrm{BXC}=\angle \mathrm{AXC}=55^{\circ}$. $\left[\right.$ As, $\left.\angle \mathrm{BXC}=\angle \mathrm{AXC}=\frac{1}{2} \angle \mathrm{BXA}=\frac{1}{2} \times 110^{\circ}=55^{\circ}\right]$

## 2. Draw a line segment $A B$ of 4 cm in length. Draw a line perpendicular to $A B$ through $A$ and $B$, respectively. Are these lines parallel?

## Solution:

Given: A line segment AB of length 4 cm .
To construct: To draw a line perpendicular to AB through A and B , respectively.

Use the following steps of construction.

1. Draw $\mathrm{AB}=4 \mathrm{~cm}$.
2. With 4 as centre and radius more than $\frac{1}{2} \mathrm{AB}$, draw an arc that is intersect AB at E .
3. With E as centre and with same radius as above draw an arc which intersect previous arc at $F$.
4. Again, taking F as centre and with same radius as above draw an arc which intersect previous arc (obtained in step ii) at G.

5. With G and F are centres, draw arcs which intersect each other at H .
6. Join $A H$. So, $A X$ is perpendicular to $A B$ at $A$. Similarly, draw $B Y \perp A B$ at $B$. Now, we know that if two lines are parallel, then the angle between them will be $0^{\circ}$ or $180^{\circ}$. So,
$\angle \mathrm{XAB}=90^{\circ}[\mathrm{XA} \perp \mathrm{AB}]$
and $\angle \mathrm{YBA}=90^{\circ}[\mathrm{YB} \perp \mathrm{AB}]$
$\angle \mathrm{XAB}+\angle \mathrm{YBA}=90^{\circ}+90^{\circ}=180^{\circ}$
Hence, the lines XA and YS are parallel. [It sum of interior angle on same side of transversal is $180^{\circ}$, then the two lines are parallel]

## 3. Draw an angle of $80^{\circ}$ with the help of a protractor. Then construct angles of (i) $40^{\circ}$ (ii) $160^{\circ}$ and (iii) $120^{\circ}$.

## Solution:

## Steps of construction:

Given: Draw an angle of $80^{\circ}$ say $\angle \mathrm{QOA}=80^{\circ}$ with the help of protractor.
Use the following steps to construct angles of:


1. With O as centre and any radius draw an arc which intersect OA at E and OO at F .
2. With E and F as centres and radius more than $\frac{1}{2}$ EF draw arcs which intersect each other at P .
3. Join OP Since, $\angle \mathrm{POA}=40^{\circ}\left[40^{\circ}=\frac{1}{2} \times 80^{\circ}\right]$
4. With F as centre and radius equal to EF draw an arc which intersect previous arc obtained in step 2 at S .
5. Join OS. Thus, $\angle \mathrm{SOA}=160^{\circ}\left[160^{\circ}=2 \times 80^{\circ}\right]$
6. With S and F as centre and radius more than $\frac{1}{2} \mathrm{SF}$ draw arcs which intersect each other at R .
7. Join OR. Thus, $\angle \mathrm{ROA}=\angle \mathrm{ROQ}=40^{\circ}+80^{\circ}=120^{\circ}$.

## 4. Construct a triangle whose sides are $3.6 \mathrm{~cm}, 3.0 \mathrm{~cm}$ and 4.8 cm . Bisect the smallest angle and measure each part.

## Solution:

To construct: a triangle ABC in which $\mathrm{AB}=3.6 \mathrm{~cm}, \mathrm{AC}=3.0 \mathrm{~cm}$ and $\mathrm{BC}=4.8 \mathrm{~cm}$, use the following steps.

1. Draw a line $\mathrm{BC}=4.8 \mathrm{~cm}$.
2. From B, point A is at a distance of 3.6 cm . So, having B as centre, draw an arc of radius 3.6 cm .

3. From C, point A is at a distance of 3 cm . So, having C as centre, draw an arc of radius 3 cm which intersect previous arc at A.
4. Join AB and AC . Therefore, ABC is the required triangle.

Where, angle B is smallest, as AC is the smallest side.

To direct angle B, we use the following steps.

1. With $B$ as centre, draw an arc intersecting AB and BC at D and E , respectively.
2. With D and E as centres and draw arcs intersecting at P .
3. Joining BP , we obtain angle bisector of $\angle \mathrm{B}$.
4. Here, $\angle \mathrm{ABC}=39^{\circ}$

Thus, $\angle \mathrm{ABD}=\angle \mathrm{DBC}=\frac{1}{2} \times 139^{\circ}=19.5^{\circ}$
5. Construct a triangle $A B C$ in which $B C=5 \mathrm{~cm}, \angle B=60^{\circ}$ and $A C+A B=$ 7.5 cm .

## Solution:

Given, in $\triangle \mathrm{ABC}, \mathrm{BC}=5 \mathrm{~cm}, \angle \mathrm{~B}=60^{\circ}$ and $\mathrm{AC}+\mathrm{AB}=7.5 \mathrm{~cm}$.
To construct: the triangle ABC use the following steps.

1. Draw the base $\mathrm{BC}=5 \mathrm{~cm}$.
2. At the point B make an $\angle \mathrm{XBC}=60^{\circ}$.
3. Cut a line segment BD equal to $\mathrm{AB}+\mathrm{AC}=7.5 \mathrm{~cm}$ from the ray BX .

4. Join DC.
5. Make an $\angle \mathrm{DCY}=\angle \mathrm{BDC}$.
6. Let CY intersect BX at A .

Therefore, ABC is the required triangle.

## 6. Construct a square of side $\mathbf{3} \mathbf{c m}$.

## Solution:

As we know that, each angle of a square is right angle that is $90^{\circ}$.
To construct: a square of side 3 cm , use the following steps.

1. Take $\mathrm{AB}=3 \mathrm{~cm}$.
2. Now, draw an angle of $90^{\circ}$ at points $A$ and $B$ and plot the parallel lines $A X$ and $B Y$ at these points.
3. Cut AD and SC of length 3 cm from AX and BY, respectively.
4. Draw $90^{\circ}$ at any one of the point C or D and join both points by CD of length 3 cm . Therefore, ABCD is the required square of side, 3 cm .


## 7. Construct a rectangle whose adjacent sides are of lengths 5 cm and 3.5

 cm.
## Solution:

As, we know that, each angle of a rectangle is right angle that is $90^{\circ}$ and its opposite sides are equal and parallel.
To construct: a rectangle whose adjacent sides are of lengths 5 cm and 3.5 cm , use the 1 following steps

1. Take BC $=5 \mathrm{~cm}$.
2. Draw $90^{\circ}$ at points B and C of the line segment BC and plot the parallel lines BX and CY at these points.

3. Cut AB and CD of length 3.5 cm from BX and CY , respectively.
4. Draw an angle $90^{\circ}$ at one of the point A or D and join both points by a line segment AD of length 5 cm .
Therefore, ABCD is the required rectangle with adjacent sides of length 5 cm and 3.5 cm .

## 8. Construct a rhombus whose side is of length 3.4 cm and one of its angles is $45^{\circ}$.

## Solution:

As, we know that, in rhombus all sides are equal.

To construct a rhombus whose side is of length 3.4 cm and one of its angle is $45^{\circ}$.

1. Taking $\mathrm{AB}=3.4 \mathrm{~cm}$.
2. AT point A and B , construct $\angle B A M=45^{\circ}$ and $\angle T B P=45^{\circ}$, respectively.
3. From AM cut off $\mathrm{AD}=3.4 \mathrm{~cm}$ and from BP cut off $\mathrm{BC}=3.4 \mathrm{~cm}$.

4. Join $\mathrm{AD}, \mathrm{DC}$ and $\mathrm{BC} . \mathrm{ABCD}$ is the required rhombus.

## Exercise No. 11.4

## Long Answer Questions:

## Construct each of the following and give justification:

## 1. A triangle if its perimeter is $\mathbf{1 0 . 4} \mathbf{~ c m}$ and two angles are $45^{\circ}$ and $120^{\circ}$.

## Solution:

Let ABC be a triangle.
Given: Perimeter $=10.4 \mathrm{~cm}$ that is, $\mathrm{AB}+\mathrm{BC}+\mathrm{CA}=10.4 \mathrm{~cm}$ and two angles are $45^{\circ}$ and $120^{\circ}$.
So, $\angle \mathrm{B}=45^{\circ}$ and $\angle \mathrm{C}=120^{\circ}$
Now, to construct the triangle ABC use the following steps.

1. Draw XY and equal to perimeter that is, $\mathrm{AB}+\mathrm{BC}+\mathrm{CA}=10.4 \mathrm{~cm}$.

2. Draw $\angle \mathrm{LXY}=\angle \mathrm{B}=45^{\circ}$ and $\angle \mathrm{MYX}=\angle \mathrm{C}=120^{\circ}$.
3. Bisect $\angle L X Y$ and $\angle M Y X$ and let these bisectors intersect at a point A.
4. Draw perpendicular bisectors PQ and RS of AX and AY , respectively.
5. Let $P Q$ intersect $X Y$ at $B$ and $R S$ intersect $X Y$ at $C$. Join $A B$ and $A C$. Therefore, $A B C$ is the required triangle.

Justification:
B lies on the perpendicular bisector PQ of AX .
Thus, $\mathrm{AB}+\mathrm{BC}+\mathrm{CA}=\mathrm{XB}+\mathrm{BC}+\mathrm{CY}=\mathrm{XY}$
Again, $\angle \mathrm{BAX}=\angle \mathrm{AXB}[\mathrm{As}, \mathrm{AB}=\mathrm{XB}] \ldots(\mathrm{I})$

Also, $\angle \mathrm{ABC}=\angle \mathrm{BAX}+\angle \mathrm{AXB} \quad[\angle \mathrm{ABC}$ is an exterior angle of $\triangle \mathrm{AXB}]$
$=\angle \mathrm{AXB}+\angle \mathrm{AXB}$ [From equation (I)]

$$
=2 \angle \mathrm{AXB}=\angle \mathrm{LXY}[\mathrm{AX} \text { is a bisector of } \angle \mathrm{LXB}]
$$

Also, $\angle \mathrm{CAY}=\angle \mathrm{AYC}[\mathrm{As}, \mathrm{AC}=\mathrm{CY}]$
$\angle \mathrm{ACB}=\angle \mathrm{CAY}+\angle \mathrm{AYC}[\angle \mathrm{ACB}$ is an exterior angle of triangle AYC]
$=\angle \mathrm{CAY}+\angle \mathrm{CAY}$
$=2 \angle \mathrm{CAY}=\angle \mathrm{MYX}$ [AY is a bisector of $\angle \mathrm{MYX}$ ]
Therefore, our construction is justified.

## 2. A triangle PQR given that $\mathrm{QR}=3 \mathrm{~cm}, \angle \mathrm{PQR}=45^{\circ}$ and $\mathrm{QP}-\mathrm{PR}=\mathbf{2 c m}$.

## Solution:

Given: in triangle $\mathrm{PQR}, \mathrm{QR}=3 \mathrm{~cm}, \angle \mathrm{PQR}=45^{\circ}$ and $\mathrm{QP}-\mathrm{PR}=2 \mathrm{~cm}$
As, C lies on the perpendicular bisector RS of AY.
To construct: a triangle PQR .
Use the following steps of construction.

1. Draw $\mathrm{QR}=3 \mathrm{~cm}$.
2. Make an angle $\mathrm{XQR}=45^{\circ}$ at point Q of base QR .
3. Cut the line segment $\mathrm{QS}=\mathrm{QP}-\mathrm{PR}=2 \mathrm{~cm}$ from the ray QX .

4. Join SR and draw the perpendicular bisector of SR say AB .
5. Let bisector AB intersect QX at P . Join PR Thus, $\triangle \mathrm{PQR}$ is the required triangle.

Justification:
Base QR and $\angle \mathrm{PQR}$ are drawn as given.
As, the point $P$ lies on the perpendicular bisector of SR.
PS = PR
Now, $\mathrm{QS}=\mathrm{PQ}-\mathrm{PS}$

$$
=P Q-P R
$$

Therefore, our construction is justified.

## 3. A right triangle when one side is 3.5 cm and sum of other sides and the hypotenuse is 5.5 cm .

## Solution:

In the right triangle $A B C$, given $B C=3.5 \mathrm{~cm}, \angle B=90^{\circ}$ and sum of other side and hypotenuse be, $\mathrm{AB}+\mathrm{AC}=5.5 \mathrm{~cm}$.
To construct a triangle ABC use the following steps

1. Draw $\mathrm{BC}=3.5 \mathrm{~cm}$
2. Make an angle $\mathrm{XBC}=90^{\circ}$ at the point B of base BC .

3. Cut the line segment BD equal to $\mathrm{AB}+\mathrm{AC}$ i.e., 5.5 cm from the ray XB .
4. Join DC and make an $\angle \mathrm{DCY}$ equal to $\angle \mathrm{BDC}$.
5. Let Y intersect BX at A .

Therefore, ABC is the required triangle.

## Justification:

Base BC and $\angle \mathrm{B}$ are drawn as given.
In $\triangle \mathrm{ACD}, \angle \mathrm{ACD}=\angle \mathrm{ADC}$ [by construction]
$\mathrm{AD}=\mathrm{AC} \ldots(\mathrm{I})$ [sides opposite to equal angles are equal]
Now, $\mathrm{AB}=\mathrm{BD}-\mathrm{AD}=\mathrm{BD}-\mathrm{AC}[$ From equation (I)]
$\mathrm{BD}=\mathrm{AB}+\mathrm{AC}$
Hence, our construction is justified.

## 4. An equilateral triangle if its altitude is $\mathbf{3 . 2} \mathbf{~ c m}$.

## Solution:

As, in an equilateral triangle all sides are equal and all angles are equal i.e., each angle is of $60^{\circ}$.
Given: altitude of an equilateral triangle say ABC is 3.2 cm .
To construct the triangle ABC use the following steps.

1. Draw a line PQ .
2. Take a point D on PQ and draw $\mathrm{DE} \perp \mathrm{PQ}$.
3. Cut AD of length 3.2 cm from DE .
4. Make angles equal to $30^{\circ}$ at A on both sides of AD say $\angle \mathrm{CAD}$ and $\angle \mathrm{BAD}$, where B and C lie on PQ.
5. Cut DC from PQ such that $\mathrm{DC}=\mathrm{BD}$

## Join AC

Hence, ABC is the required triangle.


Justification:

$$
\text { Here, } \begin{aligned}
\angle \mathrm{A} & =\angle \mathrm{BAD}+\angle \mathrm{CAD} \\
& =30^{\circ}+30^{\circ} \\
& =60^{\circ} .
\end{aligned}
$$

Also, $\mathrm{AD} \perp \mathrm{SC}$
So, $\angle \mathrm{ADS}=90^{\circ}$.
In triangle $\mathrm{ABD}, \angle \mathrm{BAD}+\angle \mathrm{DBA}=180^{\circ}$ [angle sum property]

$$
30^{\circ}+90^{\circ}+\angle \mathrm{DBA}=180^{\circ}\left[\angle \mathrm{BAD}=30^{\circ}, \text { by construction }\right]
$$

$$
\angle \mathrm{DBA}=60^{\circ}
$$

Also, $\angle \mathrm{DCA}=60^{\circ}$
Therefore, $\angle \mathrm{A}=\angle \mathrm{B}=\angle \mathrm{C}=60^{\circ}$
Hence, ABC is an equilateral triangle.

## 5. A rhombus whose diagonals are 4 cm and 6 cm in lengths.

## Solution:

As, all sides of a rhombus are equal and the diagonals of a rhombus are perpendicular bisectors of one another. So, to construct a rhombus whose diagonals are 4 cm and 6 cm . Use the following steps.

1. Draw $\mathrm{AC}=4 \mathrm{~cm}$
2. With A and C as centres and radius more than $\frac{1}{2} \mathrm{AC}$ draw $\operatorname{arcs}$ on both sides of AC to intersect each other.
3. Cut both arcs intersect each other at $P$ and $Q$, then join $P Q$.
4. Let PQ intersect AC at the point O . $\mathrm{So}, \mathrm{PQ}$ is perpendicular bisector of AC .
5. Cut off 3 cm lengths from $O P$ and $O Q$, then we get points $B$ and $D$.
6. Join $A B, B C, C D$, and $D A$. Hence, ABCD is the required rhombus.


Justification
D and B lie on perpendicular bisector of AC .
$\mathrm{DA}=\mathrm{DC}$ and $\mathrm{BA}=\mathrm{BC} \ldots$ (I)
[since, every point on perpendicular bisector of line segment is equidistant from end points of line segment]
Now, $\angle \mathrm{DOC}=90^{\circ}$
Also, $\mathrm{OD}=\mathrm{OB}=3 \mathrm{~cm}$
Thus, AC is perpendicular bisector or BD .
$\mathrm{CD}=\mathrm{CB} \ldots$ (II)
$\mathrm{AB}=\mathrm{BC}=\mathrm{CD}=\mathrm{DA}$
Now, from equation (I) and (II):
ABCD is a rhombus.

