# Exercise No. 10.1

# **Multiple Choice Questions:**

Choose the correct answer from the given four options:

- 1. To divide a line segment AB in the ratio 5:7, first a ray AX is drawn so that  $\angle BAX$  is an acute angle and then at equal distances points are marked on the ray AX such that the minimum number of these points is
- (A) 8
- (B) 10
- (C) 11
- (D) 12

## **Solution:**

(D) 12

As given in the question,

A line segment AB in the ratio 5:7

So.

A:B = 5:7

We draw a ray AX making an acute angle ∠BAX,

And mark A+B points at equal distance.

A=5 and B=7

Therefore.

Minimum number of these points = A+B

= 5+7 = 12

- 2. To divide a line segment AB in the ratio 4:7, a ray AX is drawn first such that BAX is an acute angle and then points  $A_1$ ,  $A_2$ ,  $A_3$ ,.... are located at equal distances on the ray AX and the point B is joined to
- $(A) A_{12}$
- (B)  $A_{11}$
- (C)  $A_{10}$
- (D) A<sub>9</sub>

#### **Solution:**

(B)  $A_{11}$ 

As given in the question,

A line segment AB in the ratio 4:7

```
So,
A:B = 4:7
Now.
```

Draw a ray AX making an acute angle BAX

Minimum number of points located at equal distances on the ray,

AX = A + B=4+7= 11

 $A_1, A_2, A_3...$  are located at equal distances on the ray AX.

Point B is joined to the last point is  $A_{11}$ .

- 3. To divide a line segment AB in the ratio 5: 6, draw a ray AX such that \( \textstyle BAX \) is an acute angle, then draw a ray BY parallel to AX and the points  $A_1$ ,  $A_2$ ,  $A_3$ , ... and  $B_1$ ,  $B_2$ ,  $B_3$ , ... are located at equal distances on ray AX and BY, respectively. Then the points joined are Migrealutor
- (A)  $A_5$  and  $B_6$
- (B)  $A_6$  and  $B_5$
- (C)  $A_4$  and  $B_5$
- (D)  $A_5$  and  $B_4$

#### **Solution:**

(A)

A<sub>5</sub> and B<sub>6</sub>

As given in the question, A line segment AB in the ratio 5:7

So,

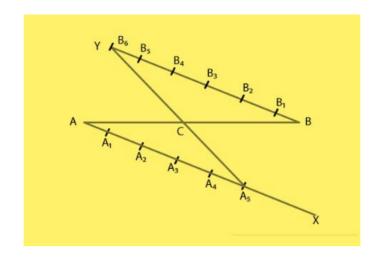
A:B = 5:7

#### Steps of construction:

- 1. Draw a ray AX, an acute angle BAX.
- 2. Draw a ray BY  $\parallel$ AX, angle ABY = angle BAX.
- 3. Now, locate the points  $A_1,A_2,A_3,A_4$  and  $A_5$  on AX and  $B_1,B_2,B_3,B_4,B_5$  and  $B_6$ (Because A: B = 5:7)
- 4. Join A<sub>5</sub>B<sub>6</sub>.

A<sub>5</sub>B<sub>6</sub> intersect AB at a point C.

AC: BC= 5:6



- 4. To construct a triangle similar to a given  $\triangle ABC$  with its sides  $\frac{3}{7}$  of the corresponding sides of  $\triangle ABC$ , first draw a ray BX such that  $\angle CBX$  is an acute angle and X lies on the opposite side of A with respect to BC. Then locate points  $B_1, B_2, B_3,...$  on BX at equal distances and next step is to join
- (A)  $B_{10}$  to C
- (B)  $B_3$  to C
- (C)  $B_7$  to C
- (**D**) B<sub>4</sub> to **C**

# **Solution:**

(C)

In this, we locate points  $B_1$ ,  $B_2$ ,  $B_3$ ,  $B_4$ ,  $B_5$ ,  $B_6$  and  $B_7$  on BX at equal distance and in next step join the last point  $B_7$  to C.

- 5. To construct a triangle similar to a given  $\triangle ABC$  with its sides  $\frac{8}{5}$  of the corresponding sides of  $\triangle ABC$  draw a ray BX such that  $\angle CBX$  is an acute angle and X is on the opposite side of A with respect to BC. The minimum number of points to be located at equal distances on ray BX is
- (A) 5
- **(B)** 8
- (C) 13
- (D)3

#### **Solution:**

(B)

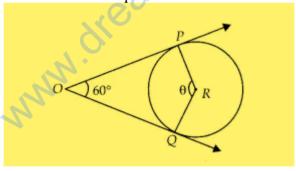
To construct a triangle similar to a given triangle, with its sides  $\frac{m}{n}$  of the n corresponding sides of given triangle the minimum number of points to be located at equal distance is equal to the greater of m and n in  $\frac{m}{n}$ . Here,  $\frac{m}{n} = \frac{8}{5}$  So, the minimum number of point to be located at equal distance on ray BX is 8.

- 6. To draw a pair of tangents to a circle which are inclined to each other at an angle of  $60^{\circ}$ , it is required to draw tangents at end points of those two radii of the circle, the angle between them should be
- (A)  $135^{\circ}$
- **(B) 90°**
- $(C) 60^{\circ}$
- **(D)**  $120^{\circ}$

# **Solution:**

(D)

The angle between them should be 120° because in that case the figure formed by the intersection point of pair of tangent, the two end points of those two radii (at which tangents are drawn) and the centre of the circle is a quadrilateral.



From figure POQR is a quadrilateral,

$$\angle POQ + \angle PRQ = 180^{\circ}$$
  
 $60^{\circ} + \theta = 180^{\circ}$   
 $\theta = 120^{\circ}$ 

[as, sum of opposite angles are 180°]

Therefore, the required angle between them is 120.

# **Short Answer Questions with Reasoning:**

Write 'True' or 'False' and justify your answer in each of the following:

1. By geometrical construction, it is possible to divide a line segment in the ratio  $\sqrt{3}$ :  $\frac{1}{\sqrt{3}}$ .

### **Solution:**

True

Explanation:

As given in the question,

Ratio= 
$$\sqrt{3}$$
:  $\frac{1}{\sqrt{3}}$ 

On solving,

$$\sqrt{3}: \frac{1}{\sqrt{3}} = 3:1$$

Required ratio = 3:1

Therefore, geometrical construction is possible to divide a line segment in the ratio 3:1.

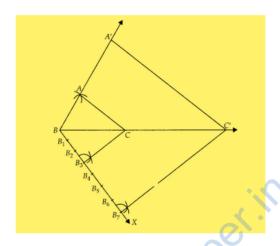
2. To construct a triangle similar to a given  $\triangle ABC$  with its sides  $\frac{7}{3}$  of the corresponding sides of  $\triangle ABC$ , draw a ray BX making acute angle with BC and X lies on the opposite side of A with respect to BC. The points  $B_1, B_2, ..., B_7$  are located at equal distances on BX,  $B_3$  is joined to C and then a line segment  $B_6C'$  is drawn parallel to  $B_3C$  where C' lies on BC produced. Finally, line segment A'C' is drawn parallel to AC.

#### **Solution:**

False

- 1. Draw a line segment BC with suitable length.
- 2. Taking B and C as centers draw two arcs of suitable radii intersecting each other at A.
- 3. Join BA and CA.  $\triangle$ ABC is the required triangle.
- 4. From B draw any ray BX downwards making an acute angle CBX.

- 5. Locate seven points  $B_1$ ,  $B_2$ ,  $B_3$ , ....  $B_7$  on BX such that  $BB_1 = B_1B_2 = B_1B_3 = B_3B_4 = B_4B_5 = B_5B_6 = B_6B_7$ .
- 6. Join  $B_3C$  and from B7 draw a line  $B7C' \parallel B3C$  intersecting the extended line segment BC at C'.
- 7. From point C' draw C'A' || CA intersecting the extended line segment BA at A'.



Then

 $\Delta A'BC'$  is the required triangle whose sides are  $\frac{7}{3}$  of the corresponding sides of  $\Delta ABC$ .

Given,

Segment B<sub>6</sub>C' is drawn parallel to B<sub>3</sub>C.

But from our construction is never possible that segment  $B_6C$ ' is parallel to  $B_3C$  because the similar triangle A'BC' has its sides  $\frac{7}{3}$  of the corresponding sides of triangle ABC.

Therefore,  $B_7C$ ' is parallel to  $B_3C$ .

# 3. A pair of tangents can be constructed from a point P to a circle of radius 3.5 cm situated at a distance of 3 cm from the centre.

#### **Solution:**

False

As, the radius of the circle is 3.5 cm

r = 3.5 cm and a point P situated at a distance of 3 cm from the centre So.

d = 3 cm.

We can see that r > d

Therefore, a point P lies inside the circle.

And, no tangent can be drawn to a circle from a point lying inside it.

# 4. A pair of tangents can be constructed to a circle inclined at an angle of $170^{\circ}$ .

# **Solution:**

True

As, the angle between the pair of tangents is always greater than 0 but less than  $180^{\circ}$ . Therefore, we can draw a pair of tangents to a circle inclined at an angle at  $170^{\circ}$ .

MMM. Healthiopper in

# **Short Answer Questions:**

# **Question:**

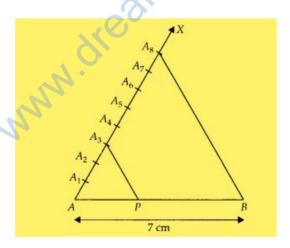
# 1. Draw a line segment of length 7 cm. Find a point P on it which divides it in the ratio 3:5.

# **Solution:**

Steps of construction:

- 1. Draw a line segment AB = 7 cm.
- 2. Draw a ray AX, making an acute ∠BAX.
- 3. Along AX, mark 3+5=8 points  $A_1, A_2, A_3, A_4, A_5, A_6, A_7, A_8$  Such that  $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_6A_7 = A_7A_8$
- 4. Join A<sub>8</sub>B.
- 5. From  $A_3$ , draw  $A_3P \parallel A_8B$  meeting AB at P. [by making an angle equal to  $\angle BA_8A$  at  $A_3$ ]

So, P is the point on AB which divides it in the ratio 3:5.



Explanation:

Let

$$AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = \dots = A_7A_8 = x$$

In  $\triangle ABA_8$ , we have

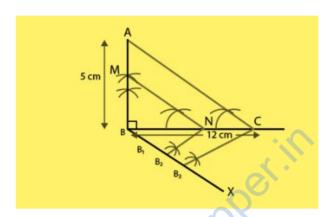
 $A_3P \parallel A_8B$ 

$$\frac{AP}{PB} = \frac{AA_3}{A_3A_8} = \frac{3x}{5x}$$

Therefore, AP: PB = 3:5

2. Draw a right triangle ABC in which BC = 12 cm, AB = 5 cm and  $\angle$ B = 90°. Construct a triangle similar to it and of scale factor  $\frac{2}{3}$ . Is the new triangle also a right triangle?

### **Solution:**

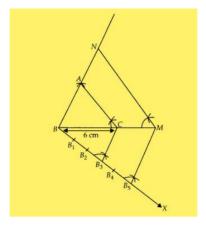


## Steps of construction:

- 1. Draw a line segment BC = 12 cm.
- 2. From B draw a line AB = 5 cm which makes right angle at B.
- 3. Join AC,  $\triangle$ ABC is the given right triangle.
- 4. From B draw an acute ∠CBX downwards.
- 5. On ray BX, mark three points  $B_1$ ,  $B_2$  and  $B_3$ , such that  $BB_1 = B_1B_2 = B_2B_3$ .
- 6. Join B<sub>3</sub>C.
- 7. From point  $B_2$  draw  $B_2N \parallel B_3C$  intersect BC at N.
- 8. From point N draw NM | CA intersect BA at M. ΔMBN is the required triangle. ΔMBN is also a right angled triangle at B.
- 3. Draw a triangle ABC in which BC = 6 cm, CA = 5 cm and AB = 4 cm. Construct a triangle similar to it and of scale factor  $\frac{5}{3}$ .

#### **Solution:**

- 1. Draw a line segment BC = 6 cm.
- 2. Taking B and C as centers, draw two arcs of radii 4 cm and 5 cm intersecting each other at A
- 3. Join BA and CA. ΔABC is the required triangle.
- 4. From B, draw any ray BX downwards making at acute angle ∠CBX
- 5. Mark five points  $B_1$ ,  $B_2$ ,  $B_3$ ,  $B_4$  and  $B_5$  on BX, such that  $BB_1 = B_1B_2 = B_2B_3 = B_3B_4 = B_4B_5$ .

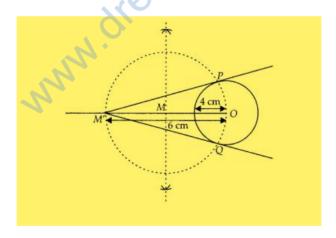


- 6. Join B<sub>3</sub>C and from B<sub>5</sub> draw B<sub>5</sub>M | B<sub>3</sub>C intersecting the extended line segment BC at M.
- 7. From point M draw MN II CA intersecting the extended line segment BA at N.

Therefore,  $\triangle NBM$  is the required triangle whose sides is equal to  $\frac{5}{3}$  of the corresponding sides of the  $\triangle ABC$ .

# 4. Construct a tangent to a circle of radius 4 cm from a point which is at a distance of 6 cm from its center.

## **Solution:**



We have, a point M' is at a distance of 6 cm from the centre of a circle of radius 4 cm. Steps of construction:

- 1. Draw a circle of radius 4 cm. Let the centre of this circle be O.
- 2. Join OM' and bisect it. Let M be mid-point of OM'.
- 3. Taking M as centre and MO as radius draw a circle to intersect circle (0, 4) at two points, P and Q.
- 4. Join PM' and QM'. PM' and QM' are the required tangents from M' to circle C(0, 4).

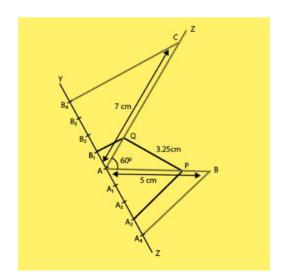
# **Long Answer Questions:**

# **Question:**

1. Two line segments AB and AC include an angle of  $60^{\circ}$  where AB = 5 cm and AC = 7 cm. Locate points P and Q on AB and AC, respectively such that  $AP = \frac{3}{4}AB$  and  $AQ = \frac{1}{4}AC$ . Join P and Q and measure the length PQ.

# **Solution:**

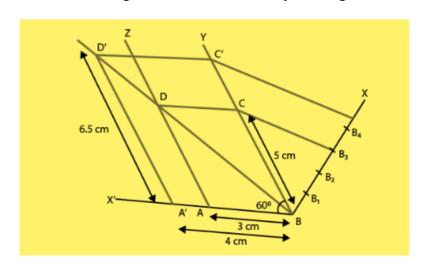
- 1. Draw a line segment AB = 5 cm.
- 2. Also, make  $\angle BAZ = 60^{\circ}$ .
- 3. With center A and radius 7 cm, draw an arc cutting the line AZ at C.
- 4. Draw a ray AX, making an acute ∠BAX.
- 5. Divide AX into four equal parts, namely  $AA_1 = A_1A_2 = A_2A_3 = A_3A_4$ .
- 6. Join  $A_4B$ .
- 7. Draw  $A_3P \parallel A_4B$  meeting AB at P.
- 8. Therefore, P is the point on AB such that  $AP = \frac{3}{4}$  AB.
- 9. Now, draw a ray AY, such that it makes an acute ∠CAY.
- 10. Divide AY into four parts, namely  $AB_1 = B_1B_2 = B_2B_3 = B_3B_4$ .
- 11. Join B<sub>4</sub>C.
- 12. Draw  $B_1Q \parallel B_4C$  meeting AC at Q. We get, Q is the point on AC such that  $AQ = \frac{1}{4} AC$ .
- 13. Join PQ and measure it.
- 14. PQ = 3.25 cm.



2. Draw a parallelogram ABCD in which BC = 5 cm, AB = 3 cm and angle  $\angle$ ABC = 60°, divide it into triangles BCD and ABD by the diagonal BD. Construct the triangle BD'C' similar to triangle BDC with scale factor  $\frac{4}{3}$ . Draw the line segment D'A' parallel to DA where A' lies on extended side BA. Is A'BC'D' a parallelogram?

#### **Solution:**

- 1. Draw a line AB=3 cm.
- 2. Now draw a ray BY making an acute ∠ABY=60°.
- 3. With centre B and radius 5 cm, draw an arc cutting the point C on BY.
- 4. Draw a ray AZ making an acute ∠ZAX'=60° (BY||AZ, as, ∠YBX'=ZAX'=60°)
- 5. With centre A and radius 5 cm, draw an arc cutting the point D on AZ.
- 6. Join CD
- 7. We obtain a parallelogram ABCD.
- 8. Join BD, the diagonal of parallelogram ABCD,
- 9. Draw a ray BX downwards making an acute ∠CBX.
- 10. Locate 4 points  $B_1$ ,  $B_2$ ,  $B_3$ ,  $B_4$  on BX, such that  $BB_1 = B_1B_2 = B_2B_3 = B_3B_4$ .
- 11. Join  $B_4C$  and from  $B_3C$  draw a line  $B_4C' \parallel B_3C$  intersecting the extended line segment BC at C'.
- 12. Draw C'D'|| CD intersecting the extended line segment BD at D'. Then,  $\Delta$ D'BC' is the required triangle whose sides are  $\frac{4}{3}$  of the corresponding sides of  $\Delta$ DBC.
- 13. Now we draw a line segment D'A' DA, where A' lies on the extended side BA.
- 14. We observe that A'BC'D' is a parallelogram in which A'D'=6.5 cm A'B = 4 cm and  $\angle$ A'BD'= 60° divide it into triangles BC'D' and A'BD' by the diagonal BD'.

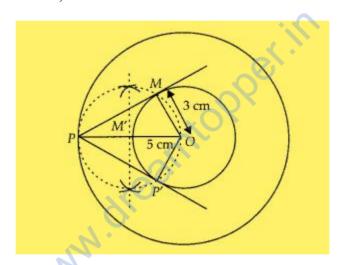


3. Draw two concentric circles of radii 3 cm and 5 cm. Taking a point on outer circle construct the pair of tangents to the other. Measure the length of a tangent and verify it by actual calculation.

#### **Solution:**

We have, two concentric circles of radii 3 cm and 5 cm with centre O. We draw pair of tangents from point P on outer circle to the other.

- 1. Draw two concentric circles with centre O and radii 3 cm and 5 cm.
- 2. Taking any point P on outer circle. Join OP.
- 3. Bisect OP, let M' be the mid-point of OP taking M' as centre and OM' as radius draw a circle dotted which cuts the inner circle at M and P'.
- 4. Join PM and PP'. Thus, PM and PP' are the required tangents.
- 5. On measuring PM and PP', we find that PM = PP' = 4 cm.



Now actual calculation: In right angle  $\Delta$ OMP,

∠PMO = 90°  
PM<sup>2</sup> = OP<sup>2</sup> – OM<sup>2</sup>  
PM<sup>2</sup> = 
$$(5)^2$$
 –  $(3)^2$   
25 – 9 = 16

PM = 4 cm

[by Pythagoras theorem]

Therefore, the length of both tangents is 4 cm.

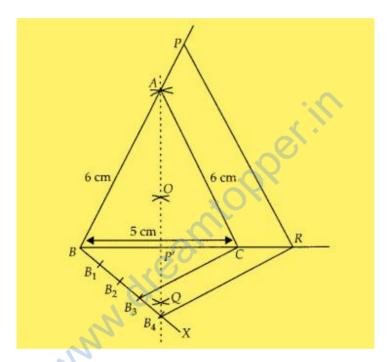
4. Draw an isosceles triangle ABC in which AB = AC = 6 cm and BC = 5 cm. Construct a triangle PQR similar to triangle ABC in which PQ = 8 cm. Also justify the construction.

#### **Solution:**

Let  $\triangle PQR$  and  $\triangle ABC$  are similar triangles, then its scale factor between the corresponding sides is  $\frac{PQ}{AB} = \frac{8}{6} = \frac{4}{3}$ 

## Steps of construction:

- 1. Draw a line segment BC = 5 cm.
- 2. Construct OQ the perpendicular bisector of line segment BC meeting BC at P'.
- 3. Taking B and C as centre we draw two arcs of equal radius 6 cm intersecting each other at A.
- 4. Join BA and CA. So,  $\triangle$ ABC is the required isosceles triangle.



- 5. From B, we draw any ray BX making an acute ∠CBX.
- 6. Locate four points  $B_1$ ,  $B_2$ ,  $B_3$  and  $B_4$  on BX such that  $BB_1 = B_1B_2 = B_2B_3 = B_3B_4$ .
- 7. Now join  $B_3C$  and from  $B_4$  draw a line  $B_4R \parallel B_3C$  intersecting the extended line segment BC at R.
- 8. From point R, draw RP \(\mathbb{\text{ CA meeting BA produced at P.}\)

Then,  $\Delta$  PBR is the required triangle.

Explanation, As, we have, B<sub>4</sub>R ll B<sub>3</sub>C

(by construction)

$$\frac{BC}{CR} = \frac{3}{1}$$
or,
$$\frac{CR}{BC} = \frac{1}{3}$$
Now,
$$\frac{BR}{BC} = \frac{BC + CR}{BC}$$

$$= 1 + \frac{CR}{BC}$$

$$= 1 + \frac{1}{3}$$

$$= \frac{4}{3}$$
And

And,

 $RP \square CA$ 

 $So, \Delta ABC \square \Delta PBR$ 

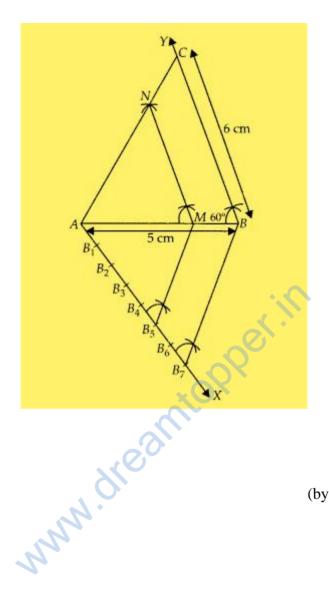
Hence,

$$\frac{PB}{AB} = \frac{RP}{CA} = \frac{BR}{BC} = \frac{4}{3}$$

5. Draw a triangle ABC in which AB = 5 cm, BC = 6 cm and ABC= 60°. Construct a triangle similar to ABC with scale factor  $\frac{5}{7}$ . Justify the construction.

### **Solution:**

- 1. Draw a line segment AB = 5 cm.
- 2. From point B, draw  $\angle ABY = 60^{\circ}$  on which take BC = 6 cm.
- 3. Join AC,  $\triangle$ ABC is the required triangle.
- 4. From A, draw any ray AX downwards making an acute angle ∠BAX
- 5. Mark 7 points  $B_1$ ,  $B_2$ ,  $B_3$ ,  $B_4$ ,  $B_5$ ,  $B_6$  and  $B_7$  on AX, such that  $AB_1 = B_1B_2 = B_2B_3 = B_3B_4 = B_1B_2 = B_2B_3 = B_3B_4 = B_1B_2 =$  $B_4B_5 = B_5B_6 = B_6B_7$ .
- 6. Join B<sub>7</sub>B and from B<sub>5</sub> draw B<sub>5</sub>M ∥ B<sub>7</sub>B intersecting AB at M.
- 7. From point M draw MN II BC intersecting AC at N. Then, ΔAMN is the required triangle whose sides are equal to  $\frac{5}{7}$  of the corresponding sides of the  $\triangle$ ABC.



Explanation:

Here,

 $B_5M \parallel B_7B$ 

$$\frac{AM}{BM} = \frac{5}{2}$$

or,

$$\frac{BM}{AM} = \frac{2}{5}$$

$$\frac{AM}{AM} = \frac{5}{AM} = \frac{AM + BM}{AM}$$
$$= 1 + \frac{BM}{AM}$$
$$= 2$$

$$=1+\frac{2}{5}$$

$$=\frac{7}{5}$$

 $Also, MN \square BC$ 

 $So, \Delta AMN \square \Delta ABC$ 

$$\frac{AM}{AB} = \frac{AN}{AC} = \frac{NM}{BC} = \frac{5}{7}$$

(by construction)

6. Draw a circle of radius 4 cm. Construct a pair of tangents to it, the angle between which is  $60^{\circ}$ . Also justify the construction. Measure the distance between the centre of the circle and the point of intersection of tangents.

### **Solution:**

Steps of construction:

- 1. Take a point O on the plane of the paper and draw a circle of radius OA = 4 cm.
- 2. Produce OA to B such that OA = AB = 4 cm.
- 3. Taking A as the centre draw a circle of radius AO = AB = 4 cm. Suppose it cuts the circle drawn in step 1 at P and Q.
- 4. Join BP and BQ to get desired tangents.

Explanation:

In  $\triangle OAP$ , we have

OA = OP = 4 cm

(Radius)

Also,

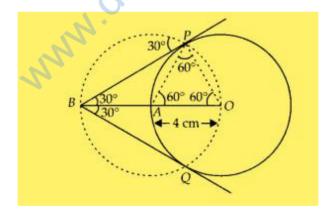
AP = 4 cm

(As, Radius of circle with centre A)

 $\Delta$ OAP is equilateral triangle.

$$\angle PAO = 60^{\circ}$$

$$\angle BAP = 120^{\circ}$$



Therefore in  $\Delta BAP$ ,

BA = AP

and  $\angle BAP = 120^{\circ}$ 

So,

$$\angle ABP = \angle APB$$

$$= 30^{\circ}$$

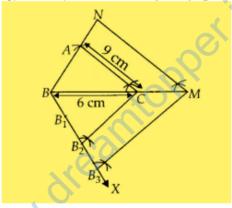
$$\angle PBQ = 60^{\circ}$$

7. Draw a triangle ABC in which AB = 4 cm, BC = 6 cm and AC = 9 cm. Construct a triangle similar to  $\triangle$ ABC with scale factor  $\frac{3}{2}$ . Justify the construction. Are the two triangles congruent? Note that all the three angles and two sides of the two triangles are equal.

#### **Solution:**

Steps of construction:

- 1. Firstly draw a line segment BC = 6 cm.
- 2. Taking B and C as centre, draw two arcs of radii 4 cm and 9 cm intersecting each other at A.
- 3. Join BA and CA. ΔABC is the required triangle.
- 4. From B, draw any ray BX downwards making an acute angle ∠CBX
- 5. Mark three points  $B_1$ ,  $B_2$ ,  $B_3$ , on BX, such that  $BB_1 = B_1B_2 = B_2B_3$ .



- 6. Join B<sub>2</sub>C and from B<sub>3</sub> draw B<sub>3</sub>M B<sub>2</sub>C intersecting BC at M.
- 7. From point M, draw MN || CA intersecting the extended line segment BA to N.

3

Then  $\triangle NBM$  is the required triangle whose sides are equal to  $\frac{3}{2}$  of the  $\triangle ABC$ .

#### Explanation:

$$B_3M \square B_2C$$

$$\frac{BC}{CM} = \frac{2}{1}$$

Now,

$$\frac{BM}{BC} = \frac{BC + CM}{BC}$$
$$= 1 + \frac{CM}{BC}$$

$$=1+\frac{1}{2}$$
$$=\frac{3}{2}$$

Also,

 $MN \square CA$ 

ΔΑΒC:ΔΝΒΜ

So,

$$\frac{NB}{AB} = \frac{NM}{AC} = \frac{BM}{BC} = \frac{3}{2}$$

The two triangles are not congruent because, if two triangles are congruent, then they have same shape and same size.

Therefore, all the three angles are same but three sides are not same that is one side is different.